# Structure of Barium Germanium Hydroxide Oxide 

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#### Abstract

BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}, M_{r}=485 \cdot 16\), monoclinic, $C c, \quad a=12.703$ (2), $\quad b=4.9047$ (7), $c=9.418$ (2) $\AA$, $\beta=105.46(2)^{\circ}, \quad V=565.50(15) \AA^{3}, \quad Z=4, \quad D_{x}=$  $124.59 \mathrm{~cm}^{-1}, F(000)=872, T=300 \mathrm{~K}, R=0.044$ for 843 independent reflections. Eight anions and one Ba cation define a regular h.c.p. layer parallel to the (201) plane. Ge atoms occupy octahedral interstices and a sheet made of three Ge octahedra is formed in the (100) plane by edge sharing. The $\mathrm{Ge}(1)$ octahedron shares four edges and the $\mathrm{Ge}(2)$ and $\mathrm{Ge}(3)$ octahedra share three. Ba is coordinated by twelve anions.


Introduction. Studies of high-pressure and hightemperature phases in the system $\mathrm{BaO}-\mathrm{GeO}_{2}$ have been carried out by Ozima, Susaki, Akimoto \& Shimizu (1982) and by Kobayashi, Ozima, Shimizu \& Akimoto (1983). Ozima et al. (1982) found three high-pressure phases in the system $\mathrm{BaO}-\mathrm{GeO}_{2}$, i.e. $\mathrm{BaGe}_{2} \mathrm{O}_{5} \mathrm{II}$, $\mathrm{BaGe}_{2} \mathrm{O}_{5}$ III, and $\mathrm{Ba}_{2} \mathrm{Ge}_{5} \mathrm{O}_{12}$. Kobayashi et al. (1983) reported two phases of perovskite-like $\mathrm{BaGeO}_{3}$, i.e. $9 R-\mathrm{BaGeO}_{3}$ and $6 \mathrm{H}-\mathrm{BaGeO}_{3} .{ }^{\prime} \mathrm{BaGe}_{3} \mathrm{O}_{7}$ ' has not been reported at atmospheric pressure or at high pressures, while the hydroxide oxide, $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$, was reported to be obtained under hydrothermal conditions ( 1000 atm and 770 K ) by Malinovskii, Pobedimskaya \& Belov (1976). As has already been pointed out (Ozima et al., 1982), the BaO component migrates from the sample through the graphite or platinum capsule during the high-pressure and high-temperature treatments. Hydrogen, on the other hand, which is contained in the pyrophyllite pressure medium, comes into the sample through the capsule. Accordingly, Ozima et al. (1982) also obtained $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$ from the high-pressure and high-temperature run product of $\mathrm{BaGeO}_{3}$ at 3 GPa and 1020 K . In these experiments, $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$ was found on the outer shell of the high-pressure and high-temperature run products of $\mathrm{BaGe}_{2} \mathrm{O}_{5}$ at 4 GPa and 1120 K .

In this paper, the structure of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$ is reported and compared with that of $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$ by Malinovskii et al. (1976).

Experimental. Parallelogram-plate crystal formed by $\{201\},\{101\}$ and $\{111\}$, volume $0.30 \times 10^{-7} \mathrm{~cm}^{3}$; Rigaku automated four-circle diffractometer, graphitemonochromated $\mathrm{Ag} K \alpha$ radiation; unit-cell parameters
from least-squares fit for 29 reflections with $30 \leq 2 \theta \leq 45^{\circ}$; integrated intensities measured by $2 \theta-\omega$ scans; 1079 measured, 843 independent reflections ( $\left.\left|F_{o}\right|>3 \sigma\left|F_{o}\right|\right)$ within $0<2 \theta \leq 50^{\circ}, 236$ unobserved; $\quad(\sin \theta / \lambda)_{\max }=0.7535 \AA^{-1}, \quad-18 \leq h \leq 18$, $0 \leq k \leq 7,0 \leq l \leq 14$; four standard reflections every fifty reflections; corrections for Lorentz-polarization, no absorption correction; heavy-atom method; fullmatrix least-squares refinement on $F$ using $R A D I E L$ (Coppens, Guru Row, Leung, Stevens, Becker \& Yang, 1979); anisotropic thermal parameters for all atoms; fully ionized scattering factors for $\mathrm{Ge}^{4+}$ and $\mathrm{Ba}^{2+}$ and $f^{\prime}, f^{\prime \prime}$ for $\mathrm{Ge}, \mathrm{Ba}$ and O from International Tables for $X$-ray Crystallography (1974), scattering factor for $\mathrm{O}^{2-}$ from Tokonami (1965); $R=0.044, w R=0.047, S$ $=1.3906, w=1$; max. $\Delta / \sigma=1 \cdot 22 ; \Delta \rho$ in final difference map $=-1.3 \sim+1.8$ e $\AA^{-3 . *}$

Discussion. Final atomic parameters are given in Table 1. The ORTEP plot (Johnson, 1965) of the structure along the $b$ axis of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$ is shown in Fig. 1. In Table 2, bond distances and bond angles are listed. As shown, Ba and Ge atoms are coordinated by 12 and 6 oxygens or hydroxide oxygens, respectively.

[^0]Table 1. Fractional coordinates $\left(\times 10^{4} ; \times 10^{3}\right.$ for O and $\mathrm{OH})$ and equivalent isotropic thermal parameters $\left(\AA^{2} \times 10^{2} ; \times 10\right.$ for O and OH$)$ with e.s.d.'s in parentheses for $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ | $z$ | $B_{\text {eq }}$ |
| Ba | 2508 (8) | 6622 (2) | -38(11) | 65 (2) |
| $\mathrm{Ge}(1)$ | 5000 | 2480 (16) | 2500 | 40 (3) |
| $\mathrm{Ge}(2)$ | 4407 (7) | 7291 (10) | 3673 (9) | 29 (8) |
| $\mathrm{Ge}(3)$ | 5560 (7) | 7603 (10) | 1241 (9) | 50 (9) |
| O(1) | 480 (3) | 436 (7) | 55 (4) | 7 (7) |
| $\mathrm{O}(2)$ | 376 (3) | 424 (8) | 270 (5) | 10 (7) |
| O(3) | 569 (3) | 583 (6) | 317 (4) | 15 (7) |
| O(4) | 430 (2) | 921 (6) | 178 (4) | 10 (6) |
| O(5) | 522 (3) | 64 (9) | 437 (5) | 20 (8) |
| O(6) | 621 (3) | 77 (8) | 218 (4) | 17 (7) |
| $\mathrm{OH}(1)$ | 689 (3) | 635 (8) | 112 (5) | 11 (7) |
| $\mathrm{OH}(2)$ | 313 (3) | 869 (10) | 391 (5) | 19 (8) |

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Fig. 1. Stereoscopic projection along the $b$ axis of the structure of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$. The $a$ axis is vertically downwards. Ba and Ge atoms are represented by thermal ellipsoids with a probability of $50 \%$. Anions are represented by a sphere of radius $0.1 \AA$. Bonds between Ba and anions are not drawn.

Table 2. Interatomic distances $(\AA)$ and interbond angles $\left({ }^{\circ}\right)$ with e.s.d.'s in parentheses for $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$

|  | Distance | $\begin{gathered} \text { Angle } \\ \mathrm{O}-M-\mathrm{O} \end{gathered}$ |  | Distance | $\begin{gathered} \text { Angle } \\ 0-M-0 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Ge}(1)$ octahedron |  |  | $\mathrm{Ge}(2)$ octahedron |  |  |
| $\mathrm{Ge}(1)-\mathrm{O}(1)$ | 2.01 (4) |  | $\mathrm{Ge}(2)-\mathrm{O}\left(1^{\prime}\right)$ | 1.89 (4) |  |
| -O(2) | 1.85 (4) |  | -O(2) | 1.83 (4) |  |
| -O(3) | 1.89 (3) |  | -O(3) | 1.95 (4) |  |
| -O(4) | 1.87 (3) |  | -O(4) | 1.99 (3) |  |
| -O(5) | 1.93 (4) |  | $-\mathrm{OH}(2)$ | 1.83 (4) |  |
| -O(6) | 1.84 (5) |  | -O(5i) | 1.96 (4) |  |
| $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.70 (6) | 88.6 (16) | $\mathrm{O}(2)-\mathrm{O}\left(1^{\prime}\right)$ | 2.74 (5) | 95.1 (16) |
| -O(3) | 2.53 (5) | 80.8 (14) | -O(3) | 2.50 (5) | 82.7 (16) |
| -O(4) | 2.92 (5) | 97.4 (14) | -O(4) | 2.74 (5) | 91.4 (15) |
| -O(6) | 2.68 (5) | 88.0 (17) | $-\mathrm{OH}(2)$ | 2.68 (6) | 94.0 (17) |
| $\mathrm{O}(5)-\mathrm{O}(2)$ | 2.74 (5) | 92.5 (18) | $\mathrm{O}\left(5^{\text {in }}\right.$ ) $-\mathrm{O}\left(1^{\text {l }}\right.$ ) | 2.80 (6) | 93.5 (16) |
| -O(3) | 2.91 (5) | 99.3 (16) | -O(3) | 2.75 (5) | 89.5 (16) |
| -O(4) | 2.51 (5) | 82.5 (16) | -O(4) | 2.51 (5) | 79.0 (15) |
| -O(6) | 2.69 (7) | 90.9 (19) | $-\mathrm{OH}(2)$ | 2.75 (5) | 93.0 (17) |
| $\mathrm{O}(3)-\mathrm{O}(2)$ | 2.50 (5) | 83.9 (15) | $\mathrm{O}\left(1^{v}\right)-\mathrm{O}(3)$ | 2.77 (6) | 92.2 (15) |
| -O(6) | 2.79 (5) | 96.8 (17) | $-\mathrm{OH}(2)$ | 2.72 (5) | 94.1 (17) |
| $\mathrm{O}\left(4^{\text {I }}\right.$ - $\mathrm{O}(2)$ | 2.77 (5) | 95.9 (15) | $\mathrm{O}(4)-\mathrm{O}(3)$ | 2.52 (4) | 79.3 (15) |
| -O(6) | $2 \cdot 47$ (5) | 83.2 (17) | - $\mathrm{OH}(2)$ | 2.82 (6) | 94.8 (16) |
| $\mathrm{Ge}(3)$ octahedron |  |  | Ba polyhedron |  |  |
| $\mathrm{Ge}(3)-\mathrm{O}(1)$ | 1.88 (3) |  | Ba-O(1) | 3.03 (4) |  |
| -O(3) | 1.98 (4) |  | -O(2) | 2.89 (4) |  |
| -O(4) | 1.96 (3) |  | -O(2ii) | 3.01 (5) |  |
| $-\mathrm{OH}(1)$ | 1.83 (4) |  | -O(3ix) | 2.77 (3) |  |
| -O(5ii) | 1.91 (4) |  | -O(4) | 2.77 (3) |  |
| -O(6) | 1.86 (4) |  | $-\mathrm{OH}\left(1^{\prime \prime}\right)$ | 2.77 (4) |  |
| $\mathrm{O}(1)-\mathrm{O}(3)$ | 2.53 (5) | 81.8 (14) | - $\mathrm{OH}\left({ }^{\text {Vii) }}\right.$ ) | 2.99 (4) |  |
| -O(4) | 2.79 (5) | 93.0 (14) | -OH(2iii) | 2.97 (5) |  |
| $-\mathrm{OH}(1)$ | 2.74 (5) | 95.2 (16) | -OH(2iv) | 2.71 (5) |  |
| -O(511) | 2.80 (6) | 95.2 (17) | -O(5 ${ }^{\text {iiii) }}$ ) | 3.02 (4) |  |
| $\mathrm{O}\left(6^{\prime \prime}\right)-\mathrm{O}(3)$ | 2.74 (5) | 90.9 (16) | -O(6) | 3.02 (5) |  |
| -O(4) | 2.47 (5) | 80.2 (16) | -O(6riii) | 2.95 (4) |  |
| -OH(1) | 2.62 (6) | 90.7 (18) |  |  |  |
| -O(5ii) | 2.69 (6) | 91.3 (18) |  |  |  |
| $\mathrm{O}(3)-\mathrm{O}(4)$ | 2.52 (4) | 79.4 (14) |  |  |  |
| $-\mathrm{OH}(1)$ | 2.77 (6) | 93.2 (17) |  |  |  |
| $\mathrm{O}\left(5^{\text {iii) }}\right.$ - ${ }^{(4)}$ | 2.81 (6) | 93.1 (16) |  |  |  |
| $-\mathrm{OH}(1)$ | 2.75 (5) | 94.8 (19) |  |  |  |

Symmetry code: (i) $+x,-1 \cdot 0+y_{1}+z$; (ii) $+x_{1}+1 \cdot 0+y_{1}+z$; (iii) $+x$, $+1.0-y,-0.5+z ;$ (iv) $+x,+2.0-y,-0.5+z$; (v) $+x,+1.0-y$, $+0.5+z$; (vi) $-0.5+x,+0.5+y,+z$; (vii) $-0.5+x,-0.5+y,+z$; (viii) $-0.5+x,+0.5-y,-0.5+z ;(\mathrm{ix})-0.5+x,+1.5-y,-0.5+z$.

In this crystal, anions together with Ba form a closest-packed layer consisting of $(8 \times \mathrm{O} / \mathrm{OH}+\mathrm{Ba})$ parallel to the (201) plane. This layer stacks to form a hexagonally close-packed structure. The repetition occurs along [201] at every sixth layer with the packing sequence ( $a b c d e f$ ), where $a, b, c, d, e f$ represent the six different phases of the closest-packed layer. Ge atoms occupy octahedral interstices and an undulating sheet of Ge octahedra is formed in the (100) plane. This sheet of Ge octahedra is made from an infinite $\left\{\mathrm{Ge}_{3} \mathrm{O}_{10}\right\}_{\infty}$ chain along the $b$ axis, which is comprised of three edge-sharing Ge octahedra. The parallel chains are interconnected by corner sharing of $O(1)$ and $O$ (5). Fig. 2(a) shows this sheet of Ge octahedra projected along the $a$ axis and in Fig. 2(b) a schematic view of the sheet in the (201) plane is shown normal to this plane. It can be easily seen in Fig. 2(b) that the $\mathrm{Ge}(1)$ octahedron shares four edges and $\mathrm{Ge}(2)$ and $\mathrm{Ge}(3)$ octahedra three. The two sets of shared edges, $\mathrm{O}(1)-\mathrm{O}(3), \mathrm{O}(2)-\mathrm{O}(3)$ and $\mathrm{O}\left(5^{\mathrm{ii})}-\mathrm{O}(4), \mathrm{O}\left(6^{\mathrm{ii}}\right)-\mathrm{O}(4)\right.$, are combined with each other via another shared edge, $\mathrm{O}(3)-\mathrm{O}(4)$.


Fig. 2. (a) Projection of a sheet of Ge octahedra along the $a$ axis of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2} .(b)$ Schematic projection of the sheet of three Ge octahedra along [201]. Thick lines indicate shared edges and $1,2,3$ indicate the $\mathrm{Ge}(1)$, the $\mathrm{Ge}(2)$ and the $\mathrm{Ge}(3)$ octahedra, respectively.

The two anions which are not shared by Ge octahedra are identified as $\mathrm{OH}^{-}$, because the bondvalence sum is 1.0 for these two. The fact that the distances $M-\mathrm{O}$ for these two are considerably smaller than those for the others supports this identification. The contribution of the hydrogen atoms to the structure factors, however, was neglected in the structure refinement.

From the fact that the $\mathrm{Ge}(1)$ octahedron shares four edges and the $\mathrm{Ge}(2)$ and $\mathrm{Ge}(3)$ octahedra three, the $\mathrm{Ge}(1)$ octahedron is expected to be most distorted. As shown in Table 2, for the $\mathrm{Ge}(1)$ octahedron, the spreads of $\mathrm{O}-\mathrm{O}$ distances and $\mathrm{O}-\mathrm{M}-\mathrm{O}$ angles are in fact larger than those in the $\mathrm{Ge}(2)$ and $\mathrm{Ge}(3)$ octahedra. Similarly to anatase (Horn, Schwerdtfeger \& Meagher, 1972), the lengths of the shared edges are prominently shorter than those of the unshared edges. However, in the case of $\mathrm{BaGe}_{2} \mathrm{O}_{5} \mathrm{II}$ (Ozima, 1985), such a tendency was not so distinctive. Three- or four-edge sharing in an octahedron in germanate is unusual but it is often seen in titanate, e.g. brookite, $\mathrm{TiO}_{2}$ (Baur, 1961) and anatase, $\mathrm{TiO}_{2}$ (Horn et al., 1972). In this respect, the present crystal could be compared to ' $\mathrm{BaTi}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$, but such a compound has not been reported. Furthermore, three- or four-edge sharing in octahedra in this crystal implies an intensive character for the covalent bonding. The structure was solved on the basis of an ionic model, which resulted in a comparatively large $\Delta \rho$ in the final difference Fourier map.

In Table 3, the structure of $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$ by Malinovskii et al. (1976) is compared with that of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$ by the present author. The former is a low-pressure (probably including atmospheric pressure) phase and the latter is a high-pressure phase. This is consistent with the differences in the density and the structure in these two phases, i.e. in $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$,

Table 3. Comparison of $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$ (present study) with $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$ (Malinovskii et al., 1976)

|  | Density <br> $\left(\mathrm{g} \mathrm{cm}^{-3}\right)$ | Ge <br> tetrahedron | Ge <br> tetragonal <br> pyramid |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{18}(\mathrm{OH})_{6}$ | 5.70 | 0 | 0 | Ge <br> $\mathrm{Ba}_{3} \mathrm{Ge}_{9} \mathrm{O}_{20}(\mathrm{OH})_{2}$ | 4.98 |

only two of the nine Ge atoms are octahedrally coordinated and the mean coordination number of Ba is 8.3. In $\mathrm{BaGe}_{3} \mathrm{O}_{6}(\mathrm{OH})_{2}$, on the other hand, all Ge atoms are octahedrally coordinated and the coordination number of Ba is 12 .

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# Structure of Lead(II) Dimercury(II) Diiodide Disulfide 

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\begin{array}{r}
\text { Abstract. } \quad \mathrm{Hg}_{2} \mathrm{PbI}_{2} \mathrm{~S}_{2}, \quad M_{r}=926 \cdot 31, \quad \text { tetragonal, } \\
P 4 / m b m, a=13 \cdot 501(1), c=4.593(1) \AA, V=837.20 \\
\AA^{3}, Z=4, D_{x}=7.349 \mathrm{~g} \mathrm{~cm}^{-3}, \lambda(\mathrm{Mo} K \alpha)=0.71069 \AA \\
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\end{array}
$$

$\mu=644.9 \mathrm{~cm}^{-1}, F(000)=1520, T=293 \mathrm{~K}$. Final $R$ $=0.039$ for 489 unique observed reflections. Crystals of $\mathrm{Hg}_{2} \mathrm{PbI}_{2} \mathrm{~S}_{2}$ were grown by annealing the proper
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[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 42700 ( 8 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

